

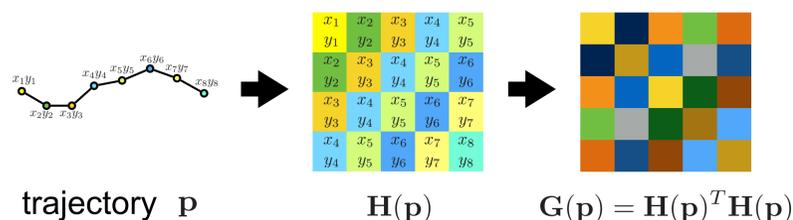
## Problem: Multi-camera motion segmentation



- Uncalibrated cameras
- Without correspondences across cameras
- No synchronization is required

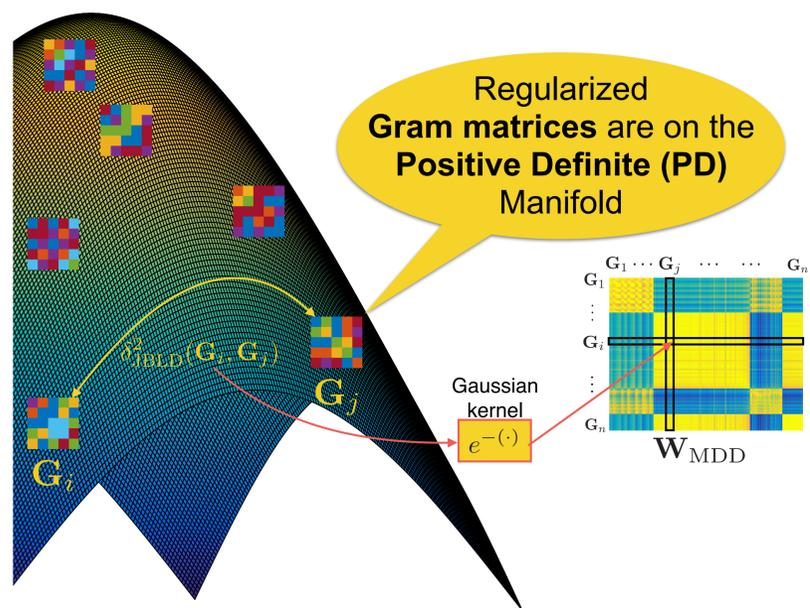
## Background

- The dynamic information is captured in its Gram matrix



## Manifold Dynamics Distance (MDD)

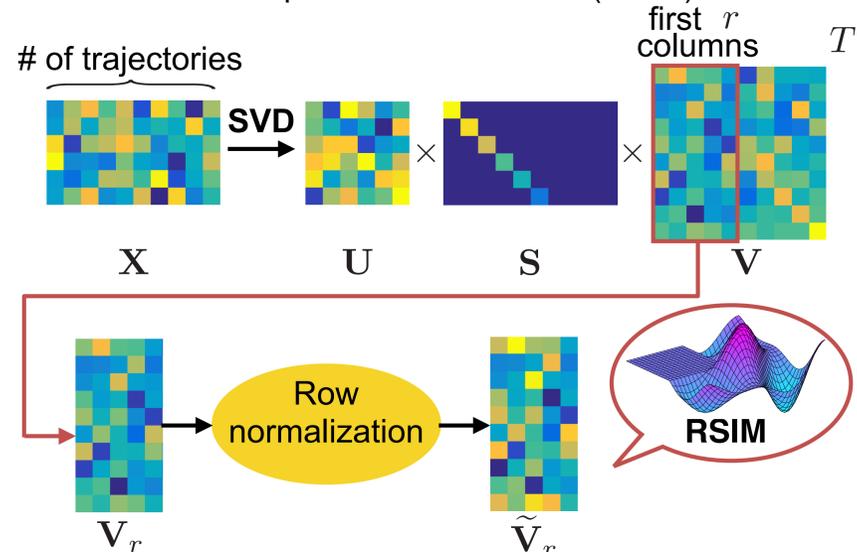
- MDD measures distance/similarity between Gram matrices (dynamics).
- JBLD is one of the most efficient MDDs.



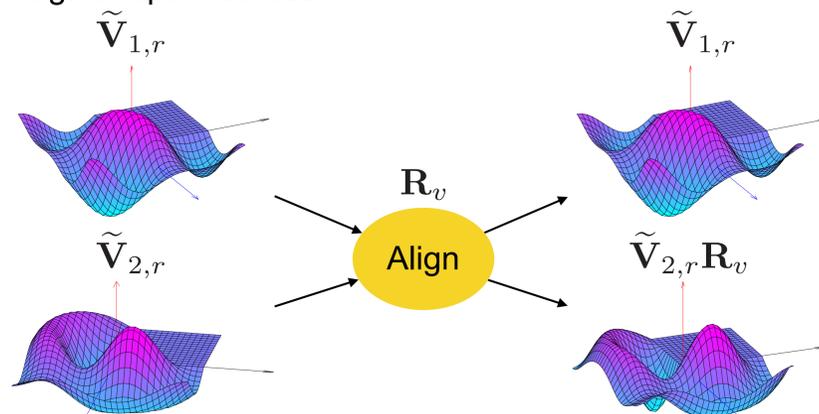
$$\delta_{\text{JBLD}}^2(\mathbf{X}, \mathbf{Y}) = \log \left| \frac{\mathbf{X} + \mathbf{Y}}{2} \right| - \frac{1}{2} \log |\mathbf{X}\mathbf{Y}|$$

## Multi-camera RSIM (McRSIM)

- Get Robust Shape Interaction Matrix (RSIM)



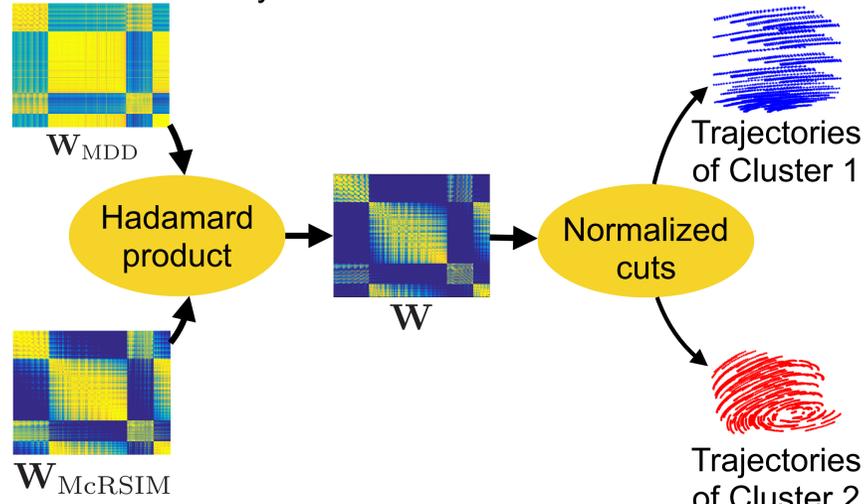
- Align shape matrices



- Compute McRSIM affinity matrix

$$\mathbf{W}_{\text{McRSIM}} = \left( \begin{bmatrix} \tilde{\mathbf{V}}_{1,r} \\ \tilde{\mathbf{V}}_{2,r} \mathbf{R}_v \end{bmatrix} \begin{bmatrix} \tilde{\mathbf{V}}_{1,r}^T & \mathbf{R}_v^T \tilde{\mathbf{V}}_{2,r}^T \end{bmatrix} \right)^\gamma$$

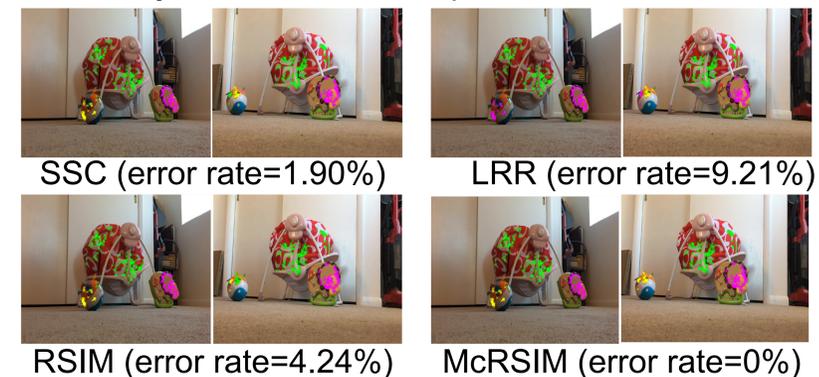
- Combine affinity matrices and cluster



## Experimental results

- New benchmark data sets RSL12 and RSL60

- Lengths of sequences are 0.5s ~ 4s
- # of trajectories in each sequence is 25 ~ 406



- Multi-camera motion segmentation

Table 1: Clustering error (in %) on RSL 12 data set. Parameters are  $r_{\min} = 1$ ,  $r_{\max} = 2$  for all RSIM and McRSIM related methods.

Methods	SSC	LRR-H2	RSIM	RSIM-MDD-LA	McRSIM	McRSIM-MDD
<b>2 motions clustering error (in %)</b>						
Mean	2.78	9.54	8.72	0.00	0.03	0.00
Median	0.00	2.91	0.20	0.00	0.00	0.00
<b>3 motions clustering error (in %)</b>						
Mean	8.36	29.55	24.08	0.00	0.00	0.00
Median	2.70	33.29	32.41	0.00	0.00	0.00
<b>Overall clustering error (in %)</b>						
Mean	5.57	19.54	16.40	0.00	0.02	0.00
Median	0.95	25.70	7.72	0.00	0.00	0.00
<b>Running time (in seconds)</b>						
Total	24.46	19.22	3.25	20.50	3.03	34.56
Avg	2.04	1.60	0.27	1.71	0.25	2.88

- With missing entries and gross contamination

Table 2: Clustering error (in %) on Hopkins 12 Real Motion Sequences With Incomplete Data. Half of the trajectories are rotated 45° and serve as Camera 2.

Methods	RSIM-M	RSIM-M-MDD	McRSIM-M	McRSIM-M-MDD
Mean	35.78	35.58	7.45	7.15
Median	38.06	37.96	1.89	1.69
Max	47.40	47.63	31.83	31.83
Std	11.63	11.45	11.45	11.58

Table 3: Clustering error (in %) on Hopkins 155 sequence with grossly contaminated entries (%5 corrupted). Half of the trajectories are rotated 45° and serve as Camera 2.

Methods	RSIM	RSIM-MDD	McRSIM	McRSIM-MDD
<b>2 motions</b>				
Mean	31.76	31.39	21.79	21.64
Median	34.66	34.05	22.52	22.19
<b>3 motions</b>				
Mean	45.05	44.77	36.13	36.02
Median	47.42	47.32	35.66	35.41
<b>Overall</b>				
Mean	34.76	34.41	25.03	24.89
Median	38.67	38.19	25.95	25.97



code & data

## Conclusion

- **Dynamics-based information** enhances performance of state-of-the-art motion segmentation methods.
- **McRSIM** is shown to be robust to rotation, translation and time delay, and performs well in multi-camera motion segmentation. It is efficient since the computational complexity is similar to that of an SVD.